## Preface

This book was written for those who want to efficiently use a computer algebra system, and Sage in particular. Symbolic computation systems offer plenty of functionality, and finding the right approach or command to solve a given problem is sometimes difficult. A reference manual provides a detailed analytic description of each function of the system; however, this is not very useful since usually we do not know in advance the name of the function we are looking for! This book provides another approach, by giving a global and synthetic point of view, while insisting on the underlying mathematics, the classes of problems we can solve, and the corresponding algorithms.

The first part, more specific to Sage, will help the reader come to grips with this system. This part is written to be understood by undergraduate students, and partly by high school students. The other parts cover more specialized topics encountered in undergraduate and graduate studies. Unlike in a reference manual, the mathematical concepts are clearly explained before illustrating them with Sage. This book is thus in the first place a book about mathematics.

To illustrate this book, Sage was a natural choice, since it is an open-source system that anybody can use, modify, and redistribute at will. In particular the student who learns Sage in high school will be able to continue to use it at undergraduate or graduate levels, in a company, etc. Sage is still a relatively young system, and despite its already extensive capacities, it does contain some bugs. However, thanks to its very active community of developers, Sage evolves very quickly. Every Sage user can report a bug—maybe together with its solution—on trac.sagemath.org or via the sage-support list.

In writing this book, we have used version 8.3 of Sage. Nevertheless, the examples should still work with later versions. However, some of the explanations may no longer hold, for example the fact that Sage relies on Maxima for numerical integrals.

When in December 2009 I asked Alexandre Casamayou, Guillaume Connan, Thierry Dumont, Laurent Fousse, François Maltey, Matthias Meulien, Marc Mezzarobba, Clément Pernet, and Nicolas Thiéry to write the first version (in French) of this book, all agreed with enthusiasm—including Nathann Cohen who joined us later on. Given the success of the French version, it was clear that an English version would be welcome. In March 2017, I decided to start working on the English version; I want to thank once again those of the "dream team" who helped me with translating the text into English, updating the examples to the new version of Sage, and moreover improving the content of the book

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(Guillaume Connan, Thierry Dumont, Clément Pernet, Nicolas Thiéry), as well as the new authors of the English version (Erik Bray, John Cremona, Marcelo Forets, Alexandru Ghitza, Hugh Thomas).

Several people had proofread the French version: Gaëtan Bisson, Françoise Jung, Hugh Thomas, Anne Vaugon, Sébastien Desreux, Pierrick Gaudry, Maxime Huet, Jean Thiéry, Muriel Shan Sei Fan, Timothy Walsh, Daniel Duparc, and especially Kévin Rowanet and Kamel Naroun. The following people helped us to improve the English version by proofreading one or several chapters, or simply reporting a typo: Fredrik Johansson, Pierre-Jean Spaenlehauer, Jacob Appelbaum, Nick Higham, Helmut Büch, Shashank Singh, Annegret Wagler, Bruno Grenet, Daniel S. Roche, Jeroen Demeyer, Evans Doe Ocansey, Minh Van Nguyen, Simon Willerton, and last but not least Adil Hasan and Dimitris Papachristoudis for their wonderful feedback. On the technical and typographic side, we thank Emmanuel Thomé, Sylvain Chevillard, Gaëtan Bisson, Jérémie Detrey, and Denis Roegel.

When writing this book, we have learned a lot about Sage, and we have of course encountered some bugs—some of which have already been fixed. We hope this book will be also useful to others: high school students, undergraduate or graduate students, engineers, researchers, or simply mathematical hobbyists. Despite several proofreadings, this book is surely not perfect, and we expect the reader to tell us about any errors or typos, or to make any suggestions, by referring to the page sagebook.gforge.inria.fr.

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